

## Article

### Procedure for Determining the Uncertainties in the Modeling of Surface Roughness in the Turning of NiTi Alloys Using the Monte Carlo Method

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**Abstract:** The paper presents a procedure for the determination of uncertainties in the modeling of surface roughness in the turning of NiTi alloys. The presented procedure is applicable both to the analysis of the measurement values of the two main roughness factors, as well as to research related to the prediction and optimization of the machining process. Type A and B, total, and expanded uncertainties were considered herein, and the obtained uncertainty values were assessed. A procedure for optimizing machining by applying the Monte Carlo (MC) method is also presented. The solutions presented in this paper are important from the point of view of practical solutions related to the prediction and optimization of the machining process. The considered procedure for determining and assessing uncertainty can be useful for the optimal selection of both machining parameters and measuring tools.

**Keywords:** surface roughness; NiTi alloy; Monte Carlo method

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## 1. Introduction

The dynamic development of science in the modern world is strongly correlated with the demand for more and more new construction materials with properties adapted to new technologies [1–5]. However, it should be remembered that the practical use of these materials is inextricably corresponded to the methods of their production and treatment. In order to manufacture new products from difficult-to-machine materials, such as shape memory alloys, titanium alloys, nickel alloys, and special ceramics, there is a need to search for more and more effective treatment methods that exceed technological barriers [6–9].

Modern machining processes, especially of difficult-to-cut materials, which are widely used in industry, should ensure the best possible quality, efficiency, economy, reliability, and environmental friendliness of products [1,3,10].

Shape memory TiNi alloys are materials with unique functional properties, but at the same time have very favorable parameters in terms of mechanical strength, fatigue strength, specific weight, resistance to corrosion and aggressive environments, etc. For this reason, there is a great interest in these materials in the industry of modern instruments or mechanical systems used in technology and medicine [11–15]. However, in order to maintain their high position as construction materials, the costs of their treatment should be reduced. The problems associated with the machining of these alloys do not allow for higher cutting parameters to be achieved, and thus impede an increase in the machining efficiency while maintaining the appropriate quality of the surface layer. The main problems

in the machining of TiNi alloys are related to high cutting temperatures and rapid tool wear, poor surface quality and cutting process efficiency, burr formation, and continuous chip, which is difficult to control [8,13,15–23].

Thus far, the priority in the industry has been to obtain the high-quality parameters of products made of NiTi alloys. The second in the hierarchy is the cost of their production. It can be expected that, in the future, due to the need to reduce and optimize production costs, research efforts will be directed toward the processes of shaping NiTi alloy elements using methods that ensure maximum efficiency while maintaining a good quality of the machined surface [6,11–13].

Due to the high requirements for elements made of NiTi alloys and the simultaneous need for effective machining of materials, the need to optimize the processes of such machining is evident. Despite the great advancement of research in the field of forecasting and optimization of the various machinability indices (surface roughness, tool wear, etc.) in relation to the processing of various construction materials, the literature lacks or highlights difficulties in finding items for which a detailed assessment of the issues related to prediction and optimization of surface roughness in the process of turning shape memory alloys has been carried out [7].

The guidelines for NiTi alloy machining presented in the scientific literature, which are based on the results of fragmentary experimental studies, are usually insufficient. In industry, cutting parameters are very often selected based on the experience of machine operators and programmers and on the recommendations of tool manufacturers in order to obtain an appropriate quality of the machined surface.

The machining process is characterized by a large number of parameters that affect it, which means that achieving optimal process efficiency while maintaining the required product quality is impossible, even for a highly qualified employee. The most unfavorable effects of this approach are the deterioration of product quality, an increase in operating costs and treatment time, a decrease in productivity, etc. [1–3,6,24].

Surface roughness is a measure of the technological quality of a product and a factor that has a large impact on the cost of production. Achieving the desired roughness value is a repetitive and empirical process that can be very time consuming. The mechanism of surface roughness formation is also very complicated and process-dependent; therefore, it is very difficult to calculate its value by using an analytical formula. The various theoretical models proposed in the relevant literature are not sufficiently accurate and are only applicable to a limited range of processes and cutting conditions, or must be used in connection with complicated diagrams or statistical tables. Therefore, an appropriate procedure is needed that can allow the surface roughness value to be assessed prior to the machining of the material, while being easy to use in industry and helping to minimize the time and cost of treatment. Moreover, such a procedure could be used to determine the appropriate cutting conditions to obtain the specific surface roughness [3,24–31].

The ability to predict surface roughness before machining has attracted great interest from many scientists, being the main goals of many research studies. The prediction of surface roughness is currently determined by using various techniques such as theoretical models [3,32–35], response surface methodology (RSM) [3,6,9,36–38], the Taguchi procedure [3,6,28,38–43], multiple linear regression equations [44], the Monte Carlo (MC) method [7,24,33,43–52], artificial intelligence through the use of the artificial neural networks (ANNs) [1,3,26,29,30,53–56], genetic algorithms (GAs) [3,57], fuzzy logic (FL) [3,36,54,58–61], the decision tree (DT) method [62], and expert systems (ES) [3]. Many research works show the use of these methods in the forecasting and optimization of surface roughness [3]. Researchers usually do not use only one modeling approach in their works, but look for a mutual compilation of the above strategies [3,6,36–39,54,59]. The benefits of using surface roughness prediction methods include an increase in the productivity and competitiveness of the production process and a simultaneous reduction in the need to re-machine a material to meet technical requirements [3,9,10,24].

Analyzing the relevant literature regarding the prediction and optimization of machining processes, it can be easily noticed that the current trend is the use of ANNs, GAs, RSM, and the Taguchi procedure for these purposes. The authors of this study note that despite the many application possibilities of the MC method [46–52], its application for solving the problems related to the prediction and optimization of machining has not been given much attention in the literature. This comment also applies to the analysis and assessment of the uncertainties [63] related to the above-mentioned prediction and optimization procedures. The developed model of surface roughness prediction together with the uncertainty determination procedure can significantly reduce the cost of machining of shape memory alloys while maintaining the optimal quality of the machined surface.

Taking into account the above literature review, this paper presents a procedure for determining the uncertainties, together with their analysis, in the modeling of surface roughness in the turning of NiTi alloys by employing the MC method. For the purposes of applying the MC method, the pseudorandom number generator with a uniform distribution was used [64]. The procedure presented here makes it possible to easily evaluate the suitability of the obtained results in the field of machining and, therefore, to choose other solutions in the event of obtaining unsatisfactory uncertainty values.

## 2. General Assumptions

Experimental tests for the purpose of determining a mathematical model were carried out for the operation of precision turning of a 6.38 mm shaft, made of the shape memory alloy -NiTi (nitinol) with the following chemical composition: 52.85 at.% Ni and 47.15 at.% Ti. Machining was carried out dry in an air atmosphere. A CCMT 060202 polycrystalline diamond (PCD) plate (Iscar, Tel Aviv-Yafo, Israel) was used for the treatment. The research plan to determine the impact of three independent factors, namely, feed ( $f$  (mm/rev)), depth of cut ( $a_p$  (mm)), and cutting speed ( $v_c$  (m/min)), on the values of the selected factors  $S_a$  and  $S_z$  (i.e., 3D areal surface texture parameters) of the surface roughness was developed according to the Taguchi experiment design guidelines (DOE) [6]. The factors  $S_a$  (i.e., the arithmetical mean height of the surface) and  $S_z$  (i.e., the maximum height of the surface—sum of the maximum peak height value and the maximum pit height value within a definition area) were defined in accordance with the standard ISO25178 [62].

Generally,  $S_a$  is represented by the equation [27]:

$$S_a = \frac{1}{LB} \int_0^L \int_0^B |z(x, y)| dx dy \quad (1)$$

where  $(x, y)$  is the deviation of the surface irregularities from the base plane, and  $L$  and  $B$  are the length and the width of the given section of surface corresponding to the baseline for the given type of surface irregularities, respectively.

The research plan is represented in the form of the so-called orthogonal table L9, which describes the individual research trials for the three factors with three different values, which are called the levels. The parameter values for the machining were selected on the basis of the generally available NiTi alloy tests. These values are:  $f = 0.038, 0.058, 0.077$  mm/rev;  $a_p = 0.03, 0.08, 0.13$  mm;  $v_c = 30, 40, 50$  m/min [6]. The 3D roughness measurements of the NiTi-treated surface were performed by using the Taylor Hobson measurement system. To perform the surface roughness measurements, a measuring tip with a rounding radius of 2  $\mu$ m was used, and the measurements were repeated ten times. The periodic nature of the surface was included for analysis, and as a result, the calculation of the selected parameters of topography was obtained. The cut-off value  $\lambda_c$  of the filter was selected based on the values recommended for periodic profiles. The value  $\lambda_c = 0.8$  mm was selected [6] based on the obtained ranges of surface roughness.

The mathematical relationships between the input data ( $f$ ,  $a_p$ , and  $v_c$ ) and the output factors ( $S_a$  and  $S_z$ ) for the Taguchi experiment were obtained here. The experimental basis for these

relationships can be found in previous work [6], while the model for determining the factors Sa and Sz was appointed using RSM.

The analysis with the Taguchi method mentioned above is only for the main factors Sa and Sz without any consideration of the correlation between them. Therefore, herein, RSM-based regression was used for the analysis of the correlation between such factors, which revealed that the contour plots of Sa were represented by corresponding curves. Therefore, the mathematical model used for predicting the suitable value was the quadratics model:

$$y = b_0 + b_1x_1 + b_2x_2 + b_3x_3 + b_4x_4 + b_{11}x_1^2 + b_{22}x_2^2 + b_{33}x_3^2 + b_{44}x_4^2 + b_{12}x_1x_2 + b_{13}x_1x_3 + b_{14}x_1x_4 + b_{23}x_2x_3 + b_{24}x_2x_4 + b_{34}x_3x_4 \quad (2)$$

where  $b_0, b_1, b_2, b_3, b_4, b_{11}, b_{22}, b_{33}, b_{44}, b_{12}, b_{13}, b_{14}, b_{23}, b_{24},$  and  $b_{34}$  are constant values, while  $x_1, x_2, x_3,$  and  $x_4$  are model parameters (i.e., input parameters).

Model (1) can be obtained by considering the full quadratics model represented by the mathematical models:

$$Sa^{mod} = 2.046 - 2.436 f - 2.038 a_p + 0.08588 v_c + 43.2 f^2 + 14.47 a_p^2 + 0.001022 v_c^2 \quad (3)$$

and

$$Sz^{mod} = 37.49 - 161.9 f - 34.25 a_p - 1.353 v_c + 1382 f^2 + 184.7 a_p^2 + 0.01612 v_c^2 \quad (4)$$

where

$$v_c = \frac{dn}{1000} \quad (5)$$

while d and n are the diameter of the machined surface and the number of rotations, respectively.

The factors  $Sa^{mod}$  and  $Sz^{mod}$  represent the arithmetical mean height and the maximum height of the surface (sum of the maximum peak height value and the maximum pit height value within a definition area), respectively. These factors describe the height or height distribution of the surface irregularities.

### 3. Results of the Measurements and Associated Uncertainties Obtained Experimentally

The predetermined values of parameters  $f, a_p$  and  $n$ , for which the factors Sa and Sz were determined with a constant value of diameter d equal to 6.380 mm, are tabulated in Table 1 (rows 1, 2, ..., 9).

Table 2 (columns  $M_s = 1, 2, \dots, 9$ ) summarizes the series of measurements of the factors Sa and Sz, which were determined for particular rows from Table 1. Each series contains  $N = 10$  measurements, while the rows described by Sa and Sz are the mean values of Sa and Sz determined on the basis of a particular n measurement. The mean Sa and Sz were adopted below as the value of the factors Sa and Sz.

The uncertainty of type A associated with the measurement of factors Sa and Sz is presented by the equation:

$$u_A(x) = \sqrt{\frac{1}{N} \sum_{n=1}^N (x_n - \bar{x})^2} \quad (6)$$

where

$$\bar{X} = \frac{1}{N} \sum_{n=1}^N x_n \quad (7)$$

corresponds to the mean  $\bar{S}_a$  and  $\bar{S}_z$  [47,63].

The uncertainty of type B associated with the measurement of factors  $S_a$  and  $S_z$  is:

$$u_B(x) = D$$

where  $D = 0.001 \text{ m}$  is the reading resolution of the above parameters.

The total and expanded uncertainties are determined based on the following formulas:

$$u(x) = \sqrt{u_A^2(x) + u_B^2(x)} \quad (9)$$

and

$$U(x) = k_p u(x) \quad (10)$$

respectively, where  $k_p$  is the coverage factor and for a distribution with a confidence level of 0.95 equal to 2 [47,63].

**Table 2.** Measurement series  $M_s$  of the factors and  $S_a$  and  $S_z$ .

| $M_s$                          | 1     | 2     | 3     | 4     | 5     | 6     | 7     | 8     | 9     |
|--------------------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| $n$                            |       |       |       |       |       |       |       |       |       |
| <b>Factor <math>S_a</math></b> |       |       |       |       |       |       |       |       |       |
| <b>[ m ]</b>                   |       |       |       |       |       |       |       |       |       |
| 1                              | 0.454 | 0.179 | 0.288 | 0.244 | 0.333 | 0.427 | 0.261 | 0.430 | 0.407 |
| 2                              | 0.404 | 0.159 | 0.278 | 0.194 | 0.363 | 0.377 | 0.351 | 0.380 | 0.387 |
| 3                              | 0.304 | 0.039 | 0.148 | 0.094 | 0.383 | 0.277 | 0.231 | 0.280 | 0.287 |
| 4                              | 0.284 | 0.049 | 0.128 | 0.074 | 0.223 | 0.257 | 0.231 | 0.260 | 0.307 |
| 5                              | 0.424 | 0.169 | 0.288 | 0.214 | 0.323 | 0.397 | 0.351 | 0.400 | 0.407 |
| 6                              | 0.414 | 0.159 | 0.258 | 0.204 | 0.313 | 0.387 | 0.361 | 0.390 | 0.387 |
| 7                              | 0.344 | 0.089 | 0.188 | 0.134 | 0.293 | 0.317 | 0.271 | 0.320 | 0.307 |
| 8                              | 0.444 | 0.189 | 0.288 | 0.234 | 0.313 | 0.417 | 0.371 | 0.420 | 0.427 |
| 9                              | 0.314 | 0.059 | 0.138 | 0.104 | 0.273 | 0.287 | 0.261 | 0.290 | 0.317 |
| 10                             | 0.354 | 0.099 | 0.178 | 0.144 | 0.213 | 0.327 | 0.321 | 0.330 | 0.337 |
| $\overline{S_a}$               | 0.374 | 0.119 | 0.218 | 0.164 | 0.303 | 0.347 | 0.301 | 0.350 | 0.357 |
| <b>Factor <math>S_z</math></b> |       |       |       |       |       |       |       |       |       |
| <b>[ m ]</b>                   |       |       |       |       |       |       |       |       |       |
| 1                              | 6.921 | 3.390 | 4.267 | 3.183 | 4.390 | 5.338 | 4.940 | 5.203 | 4.087 |
| 2                              | 6.845 | 3.312 | 4.186 | 3.105 | 4.341 | 5.197 | 4.861 | 5.081 | 4.005 |
| 3                              | 6.950 | 3.419 | 4.313 | 3.212 | 4.432 | 5.296 | 4.979 | 5.261 | 4.119 |
| 4                              | 6.864 | 3.346 | 4.214 | 3.129 | 4.327 | 5.219 | 4.882 | 5.140 | 4.036 |
| 5                              | 6.936 | 3.371 | 4.276 | 3.197 | 4.301 | 5.321 | 5.021 | 5.212 | 4.105 |
| 6                              | 6.831 | 3.340 | 4.209 | 3.083 | 4.305 | 5.181 | 4.856 | 5.114 | 4.004 |
| 7                              | 6.915 | 3.387 | 4.261 | 3.171 | 4.360 | 5.348 | 4.937 | 5.223 | 4.042 |
| 8                              | 6.963 | 3.392 | 4.312 | 3.226 | 4.412 | 5.189 | 4.867 | 5.243 | 4.137 |
| 9                              | 6.970 | 3.402 | 4.321 | 3.225 | 4.392 | 5.317 | 5.005 | 5.260 | 4.148 |
| 10                             | 6.833 | 3.275 | 4.184 | 3.112 | 4.261 | 5.158 | 4.894 | 5.081 | 4.024 |
| $\overline{S_z}$               | 6.903 | 3.363 | 4.254 | 3.164 | 4.352 | 5.256 | 4.924 | 5.179 | 4.071 |

#### 4. Modeling of Surface Roughness

Below, the modeling procedure of surface roughness based on the mathematical models given by Equations (3) and (4) and by employing the MC method, respectively, are presented in the Sections 4.1 and 4.2 . The values of parameters  $S_a$  and  $S_z$  and associated uncertainties are determined there.

##### 4.1. Calculations Based on the Mathematical Models

The values of the functions  $Sa^{mod}$  and  $Sz^{mod}$  determined based on Equations (3) and (4), as well as the associated uncertainties determined on the basis of the Equations (11)–(14) are tabulated in Table 4.

**Table 4.** Values of the functions  $Sa^{mod}$  and  $Sz^{mod}$  and the associated uncertainties.

| no. | Values of the Functions   |            | Uncertainties Based on the Mathematical Models |               |                 |               |
|-----|---------------------------|------------|--|---------------|-----------------|---------------|
|     | $Sa^{mod}$ and $Sz^{mod}$ |            |  |               |                 |               |
|     | $Sa^{mod}$                | $Sz^{mod}$ | $u_c(Sa^{mod})$                                | $U(Sa^{mod})$ | $u_c(Sz^{mod})$ | $U(Sz^{mod})$ |
|     | [ m]                      |            |  |               |                 |               |
| 1   | 0.311                     | 6.381      | 0.018  | 0.036         | 0.239           | 0.478         |
| 2   | 0.145                     | 3.446      | 0.003  | 0.006         | 0.074           | 0.148         |
| 3   | 0.257                     | 4.660      | 0.017  | 0.034         | 0.150           | 0.300         |
| 4   | 0.202                     | 3.558      | 0.012  | 0.024         | 0.232           | 0.464         |
| 5   | 0.241                     | 3.848      | 0.004  | 0.008         | 0.051           | 0.102         |
| 6   | 0.373                     | 5.326      | 0.018  | 0.036         | 0.139           | 0.278         |
| 7   | 0.328                     | 5.04       | 0.013  | 0.026         | 0.238           | 0.476         |
| 8   | 0.387                     | 5.568      | 0.005  | 0.010         | 0.072           | 0.144         |
| 9   | 0.294                     | 3.557      | 0.018  | 0.036         | 0.147           | 0.294         |

Table 4 shows that for rows 1, 5, and 9, the values of the factors  $Sa^{mod}$  and  $Sz^{mod}$  obtained on the basis of mathematical models (3) and (4) have lower values than the values of  $Sa$  and  $Sz$  obtained from the measurements. These differences are equal to a maximum of 20% and are related to the inaccuracy of determining models (3) and (4).

#### 4.2. Modeling Based on the Monte Carlo Method

The applied MC method uses a pseudo-random number generator with the uniform distribution  $U(0, 1)$  according to the Wichmann–Hill algorithm with a period equal to  $2^{121}$ . The pseudo-random number generation procedure is performed using the following six main steps [47,49,64]:

1. Create four vectors that include the integer numbers:

$$\begin{aligned}
 \mathbf{A} &= [11600 \ 47003 \ 23000 \ 33000], \\
 \mathbf{B} &= [185127 \ 45688 \ 93368 \ 65075], \\
 \mathbf{C} &= [10379 \ 10479 \ 19423 \ 8123], \\
 \mathbf{D} &= [P+456 \ P+420 \ P+300 \ P]
 \end{aligned} \tag{15}$$

where  $P = 247,483,123$ .

2. Set the four-element initial vector  $\mathbf{W}$  from the range of 0 to  $2^{31} - 1$ .
3. Calculate:

$$W_i = A_i[W_i \bmod(B_i)] \ C_i \ \text{floor}(W_i/B_i), \text{ for } i = 0, \dots, 3 \tag{16}$$

where  $A_i$ ,  $B_i$ ,  $C_i$ , and  $W_i$  denote the particular elements of the vectors  $\mathbf{A}$ ,  $\mathbf{B}$ ,  $\mathbf{C}$ , and  $\mathbf{W}$ , while the functions  $\bmod(x)$  and  $\text{floor}(x)$  denote the modulo from  $x$  and the largest integer digit no greater than  $x$ , respectively.

$10^4$ ,  $10^5$ , and  $10^6$  are checked below.



Uncertainties associated with the parameters Sa and Sz are determined based on the formula [49]:

$$u(z) = \sqrt{\frac{1}{M} \sum_{m=1}^M (z_m - \bar{z})^2} \quad (20)$$

where

$$\bar{z} = \frac{1}{M} \sum_{m=1}^M z_m \quad (21)$$

and z corresponds to the parameters Sa and Sz.

Table 5 summarizes the results of the calculations of the minimum values (rows 2 and 9) of the functions described by Equations (3) and (4) and defined by  $Sa^{MC}_{min}$  and  $Sz^{MC}_{min}$  for the case of five different numbers of MC draws (the first row):  $10^3$ ,  $10^4$ ,  $10^5$ ,  $10^6$ , and  $10^7$ . For the values of the functions  $Sa^{MC}_{min}$  and  $Sz^{MC}_{min}$  for all Monte Carlo trials, the corresponding drawing number m (rows 3 and 10),

the values of parameters f,  $a_p$ , and n (rows 4–6 and 11–13), the mean values of  $\bar{Sa}^{MC}$  and  $\bar{Sz}^{MC}$  (rows 7 and 14), and the associated uncertainties (rows 8 and 15) are determined.

**Table 5.** Calculation results of the minimum value of Equations (3) and (4) by using the MC method.

| no. | Parameters/<br>Factors | Results |        |        |        |
|-----|------------------------|---------|--------|--------|--------|
| 1   | MC [no.]               | $10^3$  | $10^4$ | $10^5$ | $10^6$ |
| 2   | $Sa^{MC}_{min}$ [m]    | 0.141   | 0.141  | 0.140  | 0.140  |
| 3   | m [no.]                | 294     | 8144   | 60915  | 692749 |
| 4   | f [mm/rev]             | 0.039   | 0.039  | 0.038  | 0.038  |
| 5   | $a_p$ [mm]             | 0.070   | 0.075  | 0.071  | 0.070  |
| 6   | n [rev/min]            | 2063    | 2123   | 2102   | 2101   |
| 7   | $\bar{Sa}^{MC}$ [m]    | 0.230   | 0.230  | 0.230  | 0.230  |
| 8   | $u_{Sa}^{MC}$ [m]      | 0.002   | 0.003  | 0.003  | 0.003  |
| 9   | $Sz^{MC}_{min}$ [m]    | 2.780   | 2.777  | 2.770  | 2.770  |
| 10  | m [no.]                | 966     | 6276   | 87578  | 179181 |
| 11  | f [mm/rev]             | 0.057   | 0.060  | 0.059  | 0.059  |
| 12  | $a_p$ [mm]             | 0.092   | 0.092  | 0.092  | 0.093  |
| 13  | n [rev/min]            | 2061    | 2065   | 2098   | 2095   |
| 14  | $\bar{Sz}^{MC}$ [m]    | 3.712   | 3.725  | 3.733  | 3.730  |
| 15  | $u_{Sz}^{MC}$ [m]      | 0.425   | 0.417  | 0.425  | 0.426  |

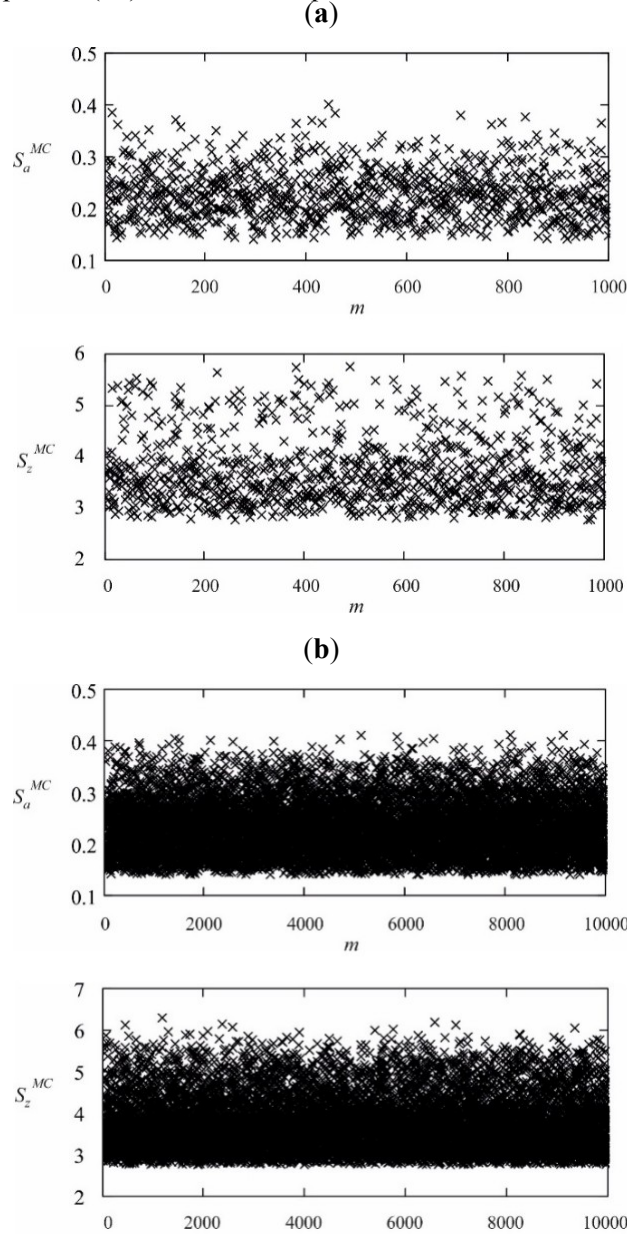
The analogous minimum values of factors  $Sa^{MC}_{min}$  and  $Sz^{MC}_{min}$  and the analogous uncertainty values of  $u_{Sa}^{MC}$  and  $u_{Sz}^{MC}$  for the number of MC draws are equal to  $10^5$  and  $10^6$ . The values

$Sa_{min}^{MC} = 0.140$  m and  $Sz_{min}^{MC} = 2.770$  m are assumed to be the optimal solutions for the MC method.

In comparison with Tables 3 and 4, Table 5 includes the following parameters:  $f$ ,  $a_p$  and  $n$  for which the lowest (optimal) values of the parameters  $Sa$  and  $Sz$  are obtained.

Tables 3 and 4 includes the values  $Sa$ ,  $Sz$ ,  $Sa^{mod}$  and  $Sz^{mod}$  as well as the associated extended uncertainties:  $U Sa$ ,  $U Sz$ ,  $U Sa^{mod}$  and  $U Sz^{mod}$  which are determined based on the measurement data and mathematical models (index: mod) for nine cases of parameters:  $f$ ,  $a_p$ , and  $n$  which are included in Table 1. The parameters,  $a_p$  and  $n$  were selected based on the Taguchi procedure. However, the results obtained for them are not optimal parameters for machining process. Only the parameters  $f$ ,  $a_p$  and  $n$ , determined on the basis of the MC method and summarized in Table 5, provide the

minimum (optimal) values of the parameters  $Sa$  and  $Sz$ . By extending the uncertainty  $\overline{U Sa}^{MC}$  from Table 5 according to Equation (10) and for MC equal to  $10^5$  or  $10^6$ , we obtain  $\overline{U Sa}^{MC} = 0.006$ .



**Figure 2.** (a) Values of factors  $Sa^{MC}$  and  $Sz^{MC}$  for the Monte Carlo trials equal to  $10^3$ . (b) Values of factors  $Sa^{MC}$  and  $Sz^{MC}$  for the Monte Carlo trials equal to  $10^4$ .

Figure 2. (a) Values of factors  $Sa^{MC}$  and  $Sz^{MC}$  for the Monte Carlo trials equal to  $10^4$ .

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The above figures show a higher concentration of random points corresponding to the values of the functions  $Sa^{MC}$  and  $Sz^{MC}$  toward their minimum values. An analogous distribution of points was obtained for MC draws equal to  $10^5$  and  $10^6$ . The reason is the syntax of the functions  $Sa^{MC}$  and  $Sz^{MC}$ , which, for a generator with a uniform distribution, provides values for these points that are close to the minimum.

## 5. Conclusions

The procedure for determining the uncertainties related to the roughness parameters presented in this paper allow for easy and quick evaluation of the obtained results related to prediction and optimization (by using the MC method) in the machining process. The results show that the uncertainties, in comparison to the measured values, have values a dozen times higher for models (3) and (4) that were determined in previous works. The reason for this is the fact that the accuracy (uncertainties) of these models was not tested in these works.

Increasing the accuracy of such models can be achieved by using RSM based on, e.g., the radial basis functions (RBFs) determined by using an ANN. In a simpler case, it is possible to use approximation polynomials with an appropriately selected order, controlled by the determination of the associated uncertainty of such modeling. For such accurate models, it is possible to use the MC method for the optimization and prediction of the machining process, as shown in this paper.

The results obtained in this paper highlight the need for a more precise determination of the factors  $Sa$  and  $Sz$  in future works. Thanks to such precise models, the value of type A uncertainty and the corresponding value of expanded uncertainty can be reduced in the optimization and prediction process of machining. An additional reduction of the expanded uncertainty is possible by reducing the value of the type B uncertainty, which can be fulfilled by increasing the resolution of the tools dedicated to machining or the resolution of the measurement devices used.

**Author Contributions:** Conceptualization, M.K.; data curation, K.T.; writing—original draft, M.K. and K.T.; formal analysis, M.K.; methodology, M.K.; writing—review and editing, M.K. and K.T.; software, M.K. and K.T. All authors have read and agreed to the published version of the manuscript.

**Funding:** This research was financially supported by the National Science Centre Poland as part of the scientific activity no. 2017/01/X/ST7/00394.

**Conflicts of Interest:** The authors declare no conflict of interest.

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